Deformation Behavior of AA8090/ TiO₂ Nanoparticulate Reinforced Metal Matrix Composites with Debonding Interfaces

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Abstract: A square array unit cell/ spherical particulate RVE models were employed to evaluate interfacial debonding using cohesive zone analysis. The particulate metal matrix composites are titanium oxide/AA8090 alloy at volume fractions of 10%, 20% and 30% TiO2. Interface debonding was observed in all the composites. The stress concentration at interface delays the occurrence of interfacial debonding

Keywords: AA8090 alloy, titanium oxide, spherical particle, RVE model, finite element analysis, interface debonding.

1. INTRODUCTION

The use of filler particles as toughening agent in composites has received considerable attention in recent years. The macroscopic response of particle reinforced composites is influenced by not only the component properties and component concentrations, but also the interfacial interaction between the particles and the matrix. In particular, the inclusion of stiff particles to a soft matrix can lead to an increase in composite stiffness, strength, impact resistance, and abrasion resistance. In contrast to the numerous experimental investigations, there have been few theoretical investigations which consider the effect of interfacial debonding in the finite deformation regime [1-14].

This paper presents a computational framework capable of capturing the influence of interfacial debonding on the finite deformation response of particle reinforced composites. The present study considers the deformation of the interface between AA8090 alloy and TiO₂ nanoparticle. Representative volume elements (RVEs) models were taken from the periodic spherical particles in a square array distribution (figure 1).

Figure 1: The RVE model.

2. MATERIALS AND METHODS

The computational framework considered in the present work is comprised of AA8090 alloy matrix material with an embedded spherical titanium oxide particle. The volume fractions of TiO₂ were 10%, 20%, and 30%. Initially, both AA8090 and TiO₂ were kept in contact with zero separation distance. PLANE183 element was used for the matrix and the nanoparticulates. The cohesive element is implemented as a linear element with four nodes. The finite element analysis was carried out for the single inclusion model undergoing a tensile load. The elastic material properties are given by $E_m = 77.0$ GPa, $E_p = 288$ GPa, $v_m = 0.33$ and $v_p = 0.29$.

Shear-log model is based on the assumption that all of the load transfer from matrix to particulate occurs via shear stresses acting on the particulate interface between the two constituents. The rate of change of the stress in the particulate to the interfacial shear stress at that point and the particulate radius, 'r' is given by:

$$
\tag{1}
$$

which may be regarded as the basic shear lag relationship.

 $\frac{d\sigma_p}{dx} = -\frac{2\tau_i}{r}$ \overline{dx}

The stress distribution in the particulate is determined by relating shear strains in the matrix around the particulate to the macroscopic strain of the composite. Some mathematical manipulation leads to a solution for the distribution of stress at a distance 'x' from the mid-point of the particulate which involves hyperbolic trig functions:

$$
\sigma_p = E_p \varepsilon_c [1 - \cosh(nx/r) \operatorname{sech}(ns)] \tag{2}
$$

where ε_c is the composite strain, *s* is the particulate aspect ratio (length/diameter) and *n* is a dimensionless constant given by:

$$
n = \left[\frac{2E_m}{E_p(1+v_m)ln(1+v_p)}\right]^{1/2}
$$
\n(3)

in which v_m is the Poisson ratio of the matrix. The variation of interfacial shear stress along the particulate length is derived, according to Equation (1), by differentiating this equation, to give:

$$
\tau_i = \frac{ne_c}{2} E_p \sinh\left(\frac{nx}{r}\right) \operatorname{sech}(ns) \tag{4}
$$

The equation for the stress in the particulate, together with the assumption of a average tensile strain in the matrix equal to that imposed on the composite, can be used to evaluate the composite stiffness. This leads to:

$$
\sigma_c = \varepsilon_c \left[v_p E_p \left(1 - \frac{\tanh(ns)}{ns} \right) + \left(1 - v_p \right) E_m \right] \tag{5}
$$

The expression in square brackets is the composite stiffness. The stiffness is a function of particulate aspect ratio, particulate/matrix stiffness ratio and particulate volume fraction.

If the particle deforms in an elastic manner (according to Hooke's law) then,

$$
\tau = \frac{n}{2}\sigma_p
$$
\n
$$
T = \frac{n}{2}\sigma_p
$$
\nIf interfacial debonding/yielding is considered to occur when the interfacial shear stress reaches its shear strength

 $\tau = \tau_{\text{max}}$ (7)

For particle/matrix interfacial fracture can be established whereby,

$$
\tau_{\text{max}} < \frac{\text{no}_p}{2} \tag{8}
$$

This approach suggests that the outcome of a matrix crack impinging on an embedded particle depends on the balance between the particle strength and the shear strength of the interface. For plane strain conditions, the macro stress- macro strain relation is as follows:

$$
\begin{Bmatrix}\n\overline{\sigma_x} \\
\overline{\sigma_y} \\
\overline{\tau_{xy}}\n\end{Bmatrix} = \begin{bmatrix}\n\overline{\mathcal{C}_{11}} & \overline{\mathcal{C}_{12}} & 0 \\
\overline{\mathcal{C}_{21}} & \overline{\mathcal{C}_{22}} & 0 \\
0 & 0 & \overline{\mathcal{C}_{33}}\n\end{bmatrix} \times \begin{Bmatrix}\n\overline{\varepsilon_x} \\
\overline{\varepsilon_y} \\
\overline{\gamma_{xy}}\n\end{Bmatrix}
$$
\n(9)

The interfacial tractions can be obtained by transforming the micro stresses at the interface as given in Eq. (3):

$$
t = \begin{cases} t_z \\ t_n \\ t_t \end{cases} = T\sigma
$$

where, $T = \begin{bmatrix} 0 & 0 & 0 \\ cos^2 \theta & sin^2 \theta & 2sin\theta cos\theta \\ -sin\theta cos\theta & sin\theta cos\theta & cos^2 \theta - sin^2 \theta \end{bmatrix}$ (10)

3. RESULTS AND DISCUSSION

The tensile and compression moduli increased with volume fraction of $TiO₂$ as shown figure 2a. The shear modulus was nearly constant with increase in the volume fraction of $TiO₂$ in the composites (figure 2b). The major Poisson's ratio increased with volume fraction of TiO₂. The stiffness mismatch between TiO₂ nanoparticulate and AA8090 alloy matrix is 211 GPa. The condition $\tau_{\text{max}} <$ no_p/2 is satisfied for the incidence of debonding in the composites including 10%, 20% and 30% TiO₂ (figure 3). The strain energy densities induced in the composites are shown in figure 4. It is observed that the strain energy density is in proportional to separation between the $TiO₂$ particle and AA8090 alloy matrix.

Figure 3: Fracture criteria of interface debonding.

Figure 4: FEA results of strain energy densities.

The normal and tangential tractions are plotted in figure 5. Because of symmetry considerations, the variations of the interface stresses with circumferential location are plotted only for the range $0^{\circ} \le \theta \le 90^{\circ}$. The normal traction in the region of interface between $TiO₂$ nanoparticulate and AA8090 alloy matrix increased with increase of volume fraction of $TiO₂$. The plots shown are for the normal traction dominated failure. The maximum allowable normal separation of the cohesive element corresponds to the separation distance at which the traction decreases to near zero value.

4. CONCLUSION

The interface debonding occurred in the composites containing 10%, 20% and 30% volume fractions boron nitride. The stress concentration at interface, which delays the occurrence of interfacial debonding, increases the energy absorption capability.

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