# Continuum Micromechanical modeling for Interfacial Debonding of TiN/AA8090 Alloy Particulate Composites

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**Abstract:** *A square array unit cell/rhombus* TiN *nanoparticle RVE models were used to predict micromechanical behavior and interfacial debonding in AA8090/* TiN *composites. The AA8090/* TiN *particulate metal matrix composites were fabricated at three different volume fractions of* TiN*. The stiffness of the composite has increased with increase of* TiN *volume fraction. The interfacial debonding was observed in the composites.* 

**Keywords:** AA8090*, titanium nitride, ellipsoidal nanoparticle, RVE model, finite element analysis, debonding.*

# **1. INTRODUCTION**

Many composite materials have high particle volume fraction, such as metal matrix composite materials reinforced with 30– 50% of ceramic particles to improve stiffness and wear resistance. These composite materials have high specific surface (i.e., high interface area per unit volume of the composite material) such that the behavior of particle/matrix interfaces may significantly influence the macroscopic behavior of composite materials. The interfacial debonding between matrix and particles is a major damage mechanism that governs nonlinear and anisotropic behavior of the composite material [1]. The interfacial debonding also governs fracture of composite materials with high particle volume fraction. The direct consequence of interfacial debonding is the decrease of modulus of the composite material as compared to that with perfect interfacial bonding. Another consequence of the interfacial debonding is the particle size effect, which has been repeatedly observed in composite materials with high particle volume fraction [2-17].

Titanium nitride (TiN) oxidizes at 800 °C at normal atmosphere. It is chemically stable at room temperature and is attacked by hot concentrated acids. A well-known use for TiN is for edge retention and corrosion resistance on machine tooling, such as drill bits and milling cutters, often improving their lifetime by a factor of three or more. TiN is classified as a 'barrier metal', even though it is clearly a ceramic from the perspective of chemistry or mechanical behavior. In the current work, AA8090 alloy/TiN nanoparticle composites were analyzed for interfacial debonding using RVE model through finite element analysis. Shape of the reinforced particle considered in this work is a rhombus. The periodic particle distribution was a square array as shown in figure 1.



**Figure 1:** A diamond RVE containing a rhombus nanoparticle.

#### **2. THEORETICAL BACKGROUND**

The strains along x- and y-directions can be determined as using the following equations:

$$
\varepsilon_{y} = -\left(\frac{v_{xy}}{\varepsilon_{x}} + \frac{1}{\varepsilon_{z}}\right)P = \frac{\Delta y}{a}
$$
\n
$$
\varepsilon_{x} = \left(\frac{1}{\varepsilon_{x}} - \frac{1}{\varepsilon_{z}}\right)P = \frac{\Delta x}{a}
$$
\n(1)\n(2)

The effective elastic moduli and Poisson's ratio in the transverse direction (xy-plane) as follows:

$$
E_x = \frac{1}{\frac{\Delta x}{Pa} + \frac{1}{E_z}} \text{ and } E_y = \frac{1}{\frac{\Delta y}{Pa} + \frac{1}{E_z}}
$$
(3)  

$$
v_{xy} = \left(\frac{\Delta y}{Pa} + \frac{1}{E_z}\right) / \left(\frac{\Delta x}{Pa} + \frac{1}{E_z}\right)
$$
(4)

Once the change in lengths along x- and y- direction ( $\Delta x$  and  $\Delta y$ ) are determined for the square RVE from the FEA,  $E_y$  and  $E_x$ and  $v_{xy}$  can be determined from Eqs. (3) and (4), correspondingly. Considering adhesion, formation of precipitates, particle size, agglomeration, voids/porosity, obstacles to the dislocation, and the interfacial reaction of the particle/matrix, the formula for the strength of composite is stated below:

$$
\sigma_{\rm c} = \left[ \sigma_{\rm m} \left\{ \frac{1 - \left( v_{\rm p} + v_{\rm v} \right)^{2/3}}{1 - 1.5 \left( v_{\rm p} + v_{\rm v} \right)} \right\} \right] e^{\rm m}_{\rm p \left( v_{\rm p} + v_{\rm v} \right)} + \text{kd}_{\rm p}^{-1/2} \tag{5}
$$
\n
$$
k = E_m m_m / E_p m_p
$$

where,  $v_v$  and  $v_p$  are the volume fractions of voids/porosity and nanoparticles in the composite respectively,  $m_p$  and  $m_m$  are the possion's ratios of the nanoparticles and matrix respectively,  $d_p$  is the mean nanoparticle size (diameter) and  $E_p$  and  $E_p$  is elastic moduli of the matrix and the particle respectively. Elastic modulus (Young's modulus) is a measure of the stiffness of a material and is a quantity used to characterize materials. Elastic modulus is the same in all orientations for isotropic materials. Anisotropy can be seen in many composites.

The upper-bound equation is given by

$$
\frac{E_{c}}{E_{m}} = \left(\frac{1 - v_{v}^{2/3}}{1 - v_{v}^{2/3} + v_{v}}\right) + \frac{1 + (\delta - 1)v_{p}^{2/3}}{1 + (\delta - 1)(v_{p}^{2/3} - v_{p})}
$$
(6)

The lower-bound equation is given by

$$
\frac{E_{c}}{E_{m}} = 1 + \frac{v_{p} - v_{p}}{\delta / (\delta - 1) - (v_{p} + v_{v})^{1/3}}
$$
(7)

where,  $\delta = E_p/E_m$ .

The transverse modulus is given by

$$
E_{t} = \frac{E_{m}E_{p}}{E_{m} + E_{p}(1 - v_{p}^{2/3})/v_{p}^{2/3}} + E_{m}(1 - v_{p}^{2/3} - v_{v}^{2/3})
$$
\n(8)

#### **3. MATERIALS METHODS**

The matrix material was AA8090 alloy. The reinforcement material was ellipsoidal TiN nanoparticles of average size 100nm. The mechanical properties of materials used in the present work are given in table 1.

Property	AA8090	TiN
Density, g/cc	2.54	5.22
Elastic modulus, GPa		251
Ultimate tensile strength, MPa	440	
Poisson's ratio	0.33	

**Table 1:** Mechanical properties of AA8090 matrix and TiN nanoparticles

AA8090 alloy/TiN composites were manufactured by the stir casting process and low pressure casting technique with argon gas at 3.0 bar. The composite samples were give solution treatment and cold rolled to the predefined size of tensile specimens. The heat-treated samples were machined to get flat-rectangular specimens (figure 2) for the tensile tests. The tensile specimens were placed in the grips of a Universal Test Machine (UTM) at a specified grip separation and pulled until failure. The test speed was 2 mm/min (as for ASTM D3039). A strain gauge was used to determine elongation.

In this research, a cubical representative volume element (RVE) was implemented to analyze the tensile behavior AA8090/ TiN nanoparticle composites at three (10%, 20% and 30%) volume fractions of TiN. The large strain PLANE183 element was used in the matrix in all the models. In order to model the adhesion between the matrix and the particle, a CONTACT 172 element was used.



**Figure 2:** Shape and dimensions of tensile specimen

# **4. RESULTS AND DISCUSSION**

The morphology of TiN particles is shown in figure 3. The crystal structure is cubic (cF8) with octahedral coordination geometry.



**Figure 3:** Morphology of TiN.





#### **4.1 Micromechanical Behavior**

Figure 4a represents the normalized tensile strengths of the AA8090 alloy/TiN composites obtained by FEA, present mathematical model, and experimental test. The tensile strength is normalized with ultimate tensile strength of AA8090 alloy. The results obtained from present mathematical model and the experimental procedure are acceptable with a marginal difference. The stiffness of the composites increases with increase of volume fraction of TiN (figure 4b). The upper limit (UL) values computed by the present mathematical model are higher than those values obtained by the 'Role of Mixtures (ROM)'and FEA. This is because of assumption of porosity in the present mathematical model. The shear strength of the composites increases with increase in volume fraction of 20% TiN (figure 4c). The major Poisson's ratio decreases with increase of volume fraction of TiN particles (figure 4d).

#### **4.2 Fracture Analysis**

If the particle deforms in an elastic manner (according to Hooke's law) then,

$$
\tau = \frac{\mathbf{n}}{2} \sigma_{\mathbf{p}} \tag{9}
$$

(11)

where  $\sigma_p$  is the particle stress. If particle fracture occurs when the stress in the particle reaches its ultimate tensile strength,  $\sigma_{p,uts}$ , then setting the boundary condition at

$$
\sigma_p = \sigma_{p, \text{uts}}
$$
\nThe relationship between the strength of the particle and the interfacial shear stress is such that if\n
$$
(10)
$$

$$
\sigma_{P,uts} < \frac{2\tau}{n}
$$

Then the particle will fracture. From the figure 5b, it is observed that the TiN nanoparticle was not fractured as the condition in Eq. (11) is not satisfied. For the interfacial debonding/yielding to occur, the interfacial shear stress reaches its shear strength:

$$
\tau = \tau_{\text{max}}
$$
\nFor particle/matrix interfacial debonding can occur if the following condition is satisfied:

 $\tau_{\max} < \frac{n\sigma_p}{2}$ 

2 (13) It is observed from figure 5a that the interfacial debonding occurs between TiN nanoparticle and AA8090 alloy matrix as the condition in Eq.(13) is satisfied.



**Figure 5:** Criterion interfacial debonding (a) and for particle fracture (b).



**Figure 6:** Images of tensile stress obtained from FEA.

The shear stresses induced at the interface are higher than those induced in the nanoparticle. Hence, the interfacial debonding was occurred between the particle and the matrix.

## **5. CONCLUSION**

The shear stress is high at the interface leading to interfacial debonding in AA8090/TiN composites. The stiffness of the composite increases with increase of TiN reinforced particle in the matrix of AA8090 alloy.

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